

What you'll Learn About

- Finite Limits as x approaches positive or negative infinity
- End Behavior Models
- Infinite Limits as x approaches a value

* If power on top bigger $\lim \rightarrow \pm\infty$

* If power in denominator is bigger $\lim = 0$

End Behavior Model

* If powers are the same look at coefficients

P. 76
 4, 21, 22
 39-44

Find the limit as $x \rightarrow \pm\infty$

Horizontal asymptotes

4A) $\lim_{x \rightarrow \infty} \frac{x+3}{3x^3-x+1} = 0$

4B) $\lim_{x \rightarrow \infty} \frac{3x^3-x+1}{x+3} = \infty$

$\lim_{x \rightarrow \infty} \frac{x}{3x^3} = \frac{1}{3x^2} = 0$

$\lim_{x \rightarrow \infty} \frac{3x^3}{x} = 3x^2$

4C) $\lim_{x \rightarrow \infty} \frac{3x^3-x+1}{x^3+3} = 3$

4D) $\lim_{x \rightarrow \infty} \frac{5x^2-x+2}{5x^2+10} = 1$

$\lim_{x \rightarrow \infty} \frac{3x^3}{x^3} = 3$

$\lim_{x \rightarrow \infty} \frac{5x^2}{5x^2} = \frac{5}{5}$

4E) $\lim_{x \rightarrow -\infty} \frac{x^3+x-1}{x^2-5x+2} = -\infty$

$\lim_{x \rightarrow -\infty} \frac{x^3}{x^2} = x$

22A) $\lim_{x \rightarrow \infty} \left(\frac{5}{x} + 2 \right) \left(\frac{8x^2-1}{2x^2} \right)$
 $(0+2)(4)$
 8

22B) $\lim_{x \rightarrow -\infty} \left(\frac{5}{x} + 2 \right) \left(\frac{8x^2-1}{2x^2} \right)$
 $(0+2)(4)$
 8

Horizontal asy at $y=8$

$y=x$

22C) $\lim_{x \rightarrow \infty} \left(\frac{5}{x} + 2 \right) \left(\frac{8x-1}{2x^2} \right)$
 $(0+2)(\infty)$
 ∞ end behavior

22D) $\lim_{x \rightarrow -\infty} \left(\frac{5}{x} + 2 \right) \left(\frac{8x^3-1}{2x^2} \right)$
 $(0+2)(-\infty)$
 $-\infty$

Find the limit as x approaches a number

$$14A) \lim_{x \rightarrow 2^-} \frac{x}{x+2} =$$

$$14B) \lim_{x \rightarrow 2^+} \frac{x}{x+2} =$$

$$14C) \lim_{x \rightarrow 2} \frac{x}{x+2} =$$

Using the limits found above graph $f(x) = \frac{x}{x+2}$

Find the vertical asymptotes of the graph and then describe the behavior to the left and right of the vertical asymptote

$$30. f(x) = \frac{1-x}{2x^2-5x-3}$$

Use your results from above to sketch a graph of $f(x) = \frac{1-x}{2x^2-5x-3}$

Find the limit of the functions that involve e^x

$$3. \lim_{x \rightarrow \infty} \frac{e^{-x}}{x}$$

$$\lim_{x \rightarrow -\infty} \frac{e^{-x}}{x}$$

$$A) \lim_{x \rightarrow \infty} \frac{e^{x+2x}}{2x} =$$

$$B) \lim_{x \rightarrow -\infty} \frac{e^{x+2x}}{2x} =$$

Find the limit of the functions that involve sine and cosine

$$C) \lim_{x \rightarrow -\infty} \frac{x^3 + \cos x}{x^3}$$

$$D) \lim_{x \rightarrow +\infty} \frac{x^3 + \cos x}{x^3}$$

$$E) \lim_{x \rightarrow \infty} \sin\left(\frac{1}{x}\right)$$

$$F) \lim_{x \rightarrow \infty} \frac{\sin\left(\frac{1}{x}\right)}{1 + \frac{1}{x}}$$

Find the limit of the functions that involve absolute value

$$8A) \lim_{x \rightarrow \infty} \frac{5x-2}{|x|-1}$$

$$8B) \lim_{x \rightarrow -\infty} \frac{5x-2}{|x|-1}$$

53A) Find the limit of $f(x)$ as

a) $x \rightarrow -\infty$, b) $x \rightarrow \infty$, c) $x \rightarrow 0^+$, d) $x \rightarrow 0^-$ e) $x \rightarrow 1^-$ f) $x \rightarrow 1^+$

$$\text{If } f(x) = \begin{cases} \frac{3x-1}{2x+5} & x < 0 \\ \frac{2}{x-1} & x \geq 0 \end{cases}$$

55A) Sketch a graph of a function that satisfies the following conditions.

$$\lim_{x \rightarrow 0} f(x) = 2$$

$$\lim_{x \rightarrow -2^-} f(x) = \infty$$

$$\lim_{x \rightarrow -2^+} f(x) = -\infty$$

$$\lim_{x \rightarrow -\infty} f(x) = 2$$

$$\lim_{x \rightarrow \infty} f(x) = -3$$

$$\lim_{x \rightarrow 3^-} f(x) = \infty$$

$$\lim_{x \rightarrow 3^+} f(x) = -\infty$$

Find the limit of the functions using the sandwich theorem

Example 9 (p.65)

$$\lim_{x \rightarrow 0} \left[x^2 \sin \left(\frac{1}{x} \right) \right]$$

p.76

10) $\lim_{x \rightarrow -\infty} \frac{1 - \cos x}{x^2}$

12) $\lim_{x \rightarrow \infty} \frac{\sin x^2}{x}$

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