

Determine the limits for the piecewise function given below

$$51A. f(x) = \begin{cases} 2-x & x < 3 \\ \frac{x}{3} + 1 & x > 3 \end{cases}$$

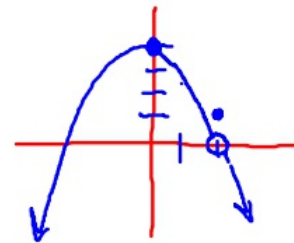
Left +
Right

a) $\lim_{x \rightarrow 3^-} f(x) = 2 - 3 = -1$ b) $\lim_{x \rightarrow 3^+} f(x) = \frac{3}{3} + 1 = 2$ c) $\lim_{x \rightarrow 3} f(x) = \text{DNE}$ d) $f(3) = \text{DNE}$

$$54A. f(x) = \begin{cases} 4 - x^2 & x \neq 2 \\ 1 & x = 2 \end{cases}$$

Parabola } Removable
Point

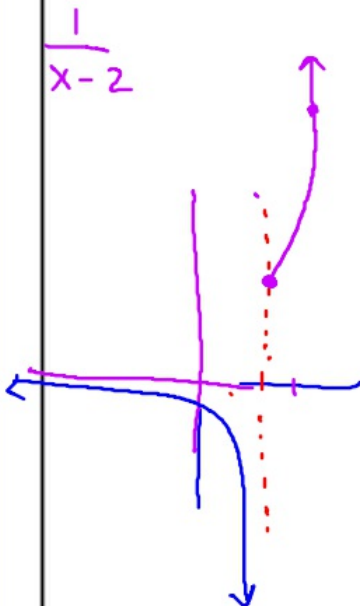
a) $\lim_{x \rightarrow 2^-} f(x) = 4 - 2^2 = 0$ b) $\lim_{x \rightarrow 2^+} f(x) = 0$ c) $\lim_{x \rightarrow 2} f(x) = 0$ d) $f(2) = 1$



$$53A. f(x) = \begin{cases} \frac{1}{x-2} & x < 2 \\ x^3 & x \geq 2 \end{cases}$$

Left
Right

a) $\lim_{x \rightarrow 2^-} f(x) = -\infty$ b) $\lim_{x \rightarrow 2^+} f(x) = 8$ c) $\lim_{x \rightarrow 2} f(x) = \text{DNE}$ d) $f(2) = 8$



Determine the Limit by substitution

$$7A) \lim_{x \rightarrow -1} 2x^2(5x+2) = -6$$

$$\frac{2(-1)^2(5(-1)+2)}{2(-3)}$$

$$13A) \lim_{x \rightarrow 30} (x-3)^{1/3} = 3$$

$$(30-3)^{1/3} = \sqrt[3]{27}$$

Determine the limit algebraically and support graphically.

$$20A) \lim_{x \rightarrow 4} \frac{x^2 - 3x - 4}{x^2 - 16} = \frac{4^2 - 3(4) - 4}{4^2 - 16} = \frac{16 - 12 - 4}{16 - 16} = \frac{0}{0}$$

$$\lim_{x \rightarrow 4} \frac{x^2 - 3x - 4}{x^2 - 16} = \frac{(x-4)(x+1)}{(x-4)(x+4)} = \frac{5}{8}$$

Removeable
Do some
Algebra

$$22A) \lim_{x \rightarrow 0} \frac{x+3}{x} - \frac{1}{3} =$$

common
denominator

$$\lim_{x \rightarrow 0} \frac{\frac{(3)}{(3)} \frac{1}{(x+3)} - \frac{1}{3} \frac{(x+3)}{(x+3)}}{x} = \frac{0}{0}$$

$$\lim_{x \rightarrow 0} \frac{\frac{3}{3(x+3)} - \frac{(x+3)}{3(x+3)}}{x}$$

$$\lim_{x \rightarrow 0} \frac{\frac{3-x-3}{3(x+3)}}{x} = \frac{\frac{-x}{3(x+3)}}{\frac{x}{1}} = \frac{-x}{3x(x+3)}$$

$$\lim_{x \rightarrow 0} \frac{-1}{3(x+3)} = \frac{-1}{3(0+3)} = \left(-\frac{1}{9}\right)$$

ONE / ∞ / $-\infty$

$\frac{12}{0} \rightarrow$ asymptotes

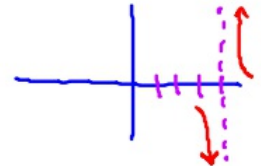
$$\frac{0}{6} = 0$$

$\frac{0}{0} \rightarrow$ Do more algebra

Determine the limit by substitution and support graphically.

$$30A) \lim_{x \rightarrow 4} \frac{x^2 - 4}{x^2 - 16} = \frac{4^2 - 4}{4^2 - 16} = \frac{16 - 4}{16 - 16} = \frac{12}{0} = \text{ONE}$$

$$\lim_{x \rightarrow 4} \frac{x^2 - 4}{x^2 - 16}$$



Left $x=4$ $y \rightarrow -\infty$ Right $x=4$ $y \rightarrow \infty$

$$x=3 \quad y = \frac{5}{-7}$$

$$x=5 \quad y = \frac{21}{9}$$

Use properties of limits to determine each limit

Assume that $\lim_{x \rightarrow 1} f(x) = 10$ and $\lim_{x \rightarrow 1} g(x) = 5$

$$A) \lim_{x \rightarrow 1} (f(x) + 3) = 10 + 3 \quad B) \lim_{x \rightarrow 1} (xg(x)) = (1)g(1) = 1(5) = 5$$

$$\lim_{x \rightarrow 1} f(x) + \lim_{x \rightarrow 1} 3$$

$$C) \lim_{x \rightarrow 1} (f^2(x)) = 10^2 = 100 \quad D) \lim_{x \rightarrow 1} \frac{f(x)}{g(x) + 2} = \frac{10}{5 + 2} = \frac{10}{7}$$