

Construct a sinusoid with the given amplitude and period that goes through the given point.

Sine

A) Amp: 6, period 8π , point (0, 0)

B) Amp: 5.5, period $\frac{\pi}{6}$, point (4, 0)

$$A = 6$$

$$\text{Per} = \frac{2\pi}{B}$$

$$B = \frac{2\pi}{\text{per}} = \frac{2\pi}{8\pi} = \frac{1}{4}$$

$$Y = 6 \sin \frac{1}{4}x$$

$$Y = A \sin B(x-c) + D$$

$$A = 5.5$$

$$B = \frac{2\pi}{\frac{\pi}{6}} = \frac{2\pi}{1} \cdot \frac{6}{\pi} = 12$$

P.S. Right 4

$$Y = 5.5 \sin 12(x-4)$$

C) Amp: 8, period 10π , point (0, 0)

$$Y = 8 \sin \frac{1}{5}x$$

$$B = \frac{2\pi}{\text{per}} = \frac{2\pi}{10\pi} = \frac{1}{5}$$

D) Amp: 4.5, period $\frac{\pi}{10}$, point (6, 0)

$$Y = 4.5 \sin 20(x-6)$$

Calculating the Ebb and Flow of Tides for Maui

February 12th, 2016, high tide occurred at 7:02 pm. At that time the water was 1.5 meters deep. Low tide occurred at 12:36 p.m, at which time the water was only .2 meters deep. Assume that the depth of the water is a sinusoidal function of time with a period of half a lunar day (about 12 hrs 24 min)

$$\frac{24}{60} = .4$$

12.4 hr

- a) Model the depth, D , as a sinusoidal function of time, t , algebraically then graph the function.

$$\text{Amp} = \frac{\text{max} - \text{min}}{2} = \frac{1.5 - .2}{2} = .65$$

$$y = .65 \cos \frac{\pi}{6.2}(x - 19.03) + .85$$

$$\text{V.s.} = \frac{\text{max} + \text{min}}{2} = \frac{1.5 + .2}{2} = .85$$

$$y = -.65 \cos \frac{\pi}{6.2}(x - 12.6) + .85$$

$$B = \frac{2\pi}{\text{per}} = \frac{2\pi}{12.4} = \frac{\pi}{6.2}$$

- b) At what time did the first low tide occur?
- c) What was the approximate depth of the water at 6:00 am and at 3:00 pm?
- d) What was the first time on this day when the water was 1 meter deep?